

Changing the Subject of a Formula

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1)

Change the subject of the formula

$$r = 3p + 2t$$

to p .

2

$$r = 3p + 2t$$

$$\begin{array}{r} -2t \\ -2t \end{array}$$

$$3p = r - 2t \quad \checkmark$$

$$\begin{array}{r} \div 3 \\ \div 3 \end{array} \quad p = \frac{r - 2t}{3} \quad \checkmark \quad \text{or} \quad p = \frac{1}{3}(r - 2t)$$

2)

Change the subject of the formula

$$P = 2(L + B)$$

to L .

2

$$\begin{array}{l} P = 2(L + B) \quad \text{OR,,} \quad P = 2(L + B) \\ \div 2 \quad \quad \div 2 \\ L + B = \frac{P}{2} \quad \checkmark \\ -B \quad \quad -B \\ L = \frac{P}{2} - B \quad \checkmark \end{array}$$
$$\begin{array}{l} P = 2L + 2B \\ -2B \quad \quad -2B \\ 2L = P - 2B \quad \checkmark \\ \div 2 \quad \quad \div 2 \\ L = \frac{P - 2B}{2} \quad \checkmark \end{array}$$

3)

$$P = R^2b - 5$$

Change the subject of the formula to R .

3

$$P = R^2b - 5$$

$$+5 \quad +5$$

$$R^2b = P + 5 \quad \checkmark$$

$$\div b \quad \div b$$
$$R^2 = \frac{P + 5}{b} \quad \checkmark$$

$$\checkmark \quad \checkmark$$
$$R = \sqrt{\frac{P + 5}{b}} \quad \checkmark$$

4)

Change the subject of the formula $m = \frac{3x+2y}{p}$ to x .

3

$$m = \frac{3x+2y}{p}$$

$$\begin{array}{c} \times p \\ \times p \end{array}$$

$$mp = 3x + 2y \quad \checkmark$$

$$\begin{array}{c} -2y \\ -2y \end{array}$$

$$3x = mp - 2y \quad \checkmark$$

$$\div 3$$

$$\div 3$$

$$x = \frac{mp - 2y}{3} \quad \checkmark \text{ or } x = \frac{1}{3}(mp - 2y)$$

5)

Change the subject of the formula

$$\frac{x}{c} + a = b$$

to x .

2

$$\begin{array}{l} \frac{x}{c} + a = b \quad \text{or} \quad \frac{x}{c} + a = b \\ \begin{array}{ccc} \times c & \times c & \times c \\ \hline x + ac = bc & \checkmark & \end{array} \\ \begin{array}{ccc} -ac & -ac & \\ \hline x = bc - ac & \checkmark & \end{array} \end{array} \quad \begin{array}{l} \frac{x}{c} + a = b \\ \begin{array}{cc} -a & -a \\ \hline \frac{x}{c} = b - a & \checkmark \\ \begin{array}{cc} \times c & \times c \\ \hline x = c(b - a) & \checkmark \end{array} \end{array} \end{array}$$

6)

Change the subject of the formula

$$A = \frac{1}{2}h(a+b)$$

to h .

2

$$A = \frac{1}{2}h(a+b)$$

$\times 2$

$\times 2$

$$2A = h(a+b) \quad \checkmark$$

$\div (a+b)$

$\div (a+b)$

$$h = \frac{2A}{a+b} \quad \checkmark$$

7)

Change the subject of the formula

$$K = \frac{m^2 n}{p}$$

to m .

3

$$\begin{aligned} K &= \frac{m^2 n}{p} \\ \overset{\times p}{K} &= \overset{\times p}{\frac{m^2 n}{p}} \quad \checkmark \\ Kp &= m^2 n \quad \checkmark \\ \overset{\div n}{m^2} &= \overset{\div n}{\frac{Kp}{n}} \quad \checkmark \\ m &= \sqrt{\frac{Kp}{n}} \quad \checkmark \end{aligned}$$

8)

A formula used to calculate lighting efficiency is

$$E = \frac{I}{D^2}$$

Change the subject of this formula to D .

3

$$\begin{aligned} E &= \frac{I}{D^2} \\ \times D^2 & \quad \times D^2 \\ ED^2 &= I \quad \checkmark \\ \div E & \quad \div E \\ D^2 &= \frac{I}{E} \quad \checkmark \\ D &= \sqrt{\frac{I}{E}} \quad \checkmark \end{aligned}$$

9)

Change the subject of the formula

$$p = q + \sqrt{a}$$

to a .

2

$$\begin{aligned} p &= q + \sqrt{a} \\ -q \quad -q \\ \sqrt{a} &= p - q \quad \checkmark \\ \text{sq} \quad \text{sq} \\ a &= (p - q)^2 \quad \checkmark \end{aligned}$$

$$\text{sq} \quad \text{sq} \quad \text{sq} \\ 25 = (2 + 3)^2 \quad \times$$

10)

Change the subject of the formula $s = ut + \frac{1}{2}at^2$ to a .

3

$$s = ut + \frac{1}{2}at^2$$

$$\times 2 \quad \times 2 \quad \times 2$$

$$2s = 2ut + at^2 \quad \checkmark$$

$$-2ut \quad -2ut$$

$$at^2 = 2s - 2ut \quad \checkmark$$

$$\div t^2 \quad \div t^2$$

$$a = \frac{2s - 2ut}{t^2} \quad \checkmark$$

11)

Change the subject of the formula $L = \sqrt{4kt - p}$ to k .

3

$$L = \sqrt{4kt - p}$$

$$\begin{array}{cc} \text{sq} & \text{sq} \\ L & \end{array}$$

$$L^2 = 4kt - p \quad \checkmark$$

$$\begin{array}{cc} +p & +p \\ 4kt & = L^2 + p \end{array} \quad \checkmark$$

$$\begin{array}{cc} \div 4t & \div 4t \\ k & = \frac{L^2 + p}{4t} \end{array} \quad \checkmark$$

